# Assignment 5

R-4.5 Suppose we are given two n-element sorted sequences A and B that should not be viewed as sets (that is, A and B may contain duplicate entries). Give an O(n)-time pseudo-code algorithm for computing a sequence representing the set A U B (with no duplicates).

|  |
| --- |
| Algorithm removeDuplicateAndUnion(A, B)  Input:sequences A and B with n elements each  Output:sorted sequence of A U B    S <- empty sequence  while !A.isEmpty() /\ !B.isEmpty() do  if B.first().element() < A.first().element() then  S.insertLast(B.remove(B.first()))  else if B.first().element() > A.first().element() then  S.insertLast(A.remove(A.first()))  else  S.insertLast(A.remove(A.first()))  B.remove(B.first())  return S |

R-4.9 Suppose we modify the deterministic version of the quick-sort algorithm so that, instead of selecting the last element in an n-element sequence as the pivot, we choose the element at rank (index) n/2,, that is, an element in the middle of the sequence. What is the running time of this version of quick-sort on a sequence that is already sorted?

Answer: because the pivot number is the middle and the sequence is sorted, it doesn’t take time for swapping, just takes time to compare the middle element with other n-1 elements, therefore the running time is O(n)

C-4.10 Suppose we are given an n-element sequence S such that each element in S represents a different vote in an election, where each vote is given as an integer representing the ID of the chosen candidate. Without making any assumptions about who is running or even how many candidates there are, design an O(n log n)-time algorithm to see who wins the election S represents, assuming the candidate with the most votes wins.

|  |
| --- |
| Algorithm findElectionWinner(S)  Input: n-element sequence S where each element represents a different vote  Output: ID of winning candidate  mergeSort(S, C)  winCandidateId <- S.first()  maxVote <- 0  prevId <- S.first()  noOfVote <- 0  while !S.isEmpty() do  curId <- S.remove(S.first())  if curId != prevId then  if maxVote < noOfVote then  maxVote <- noOfVote  winCandidateId <- curId  noOfVote <- 0  else  prevId <- curId  noOfVote <- noOfVote + 1  return winCandidateId |

Let L be a List of objects colored either red, green, or blue. Design an in-place algorithm sortRBG(L) that places all red objects in list L before the blue colored objects, and all the blue objects before the green objects. Thus the resulting List will have all the red objects followed by the blue objects, followed by the green objects. Hint: use the method swapElements to move the elements around in the List. To receive full credit, you must use positions for traversal, e.g., first, last, after, before, swapElements, etc. which is necessary to make it in-place.

|  |
| --- |
| Algorithm sortRBG(L)  Input: list S includes color objects which represent 3 colors, R, B and G  Output: list S is sorted by Red 🡪 Blue 🡪 Green  size <- L.size()  curPos <- 0  curColor <- red    for i<-0 to size - 1 do  if L.elemAtRank(i).element() <> curColor then  if i = (size – 1) then  if curColor <> Green then  if curColor = red then  curColor = blue  else  if curColor = blue then  curColor = green  else  break  i <- curPos  else  L.swapElements(curPos, i)  curPos <- curPos + 1  else  curPos <- curPos + 1 |